

FIGURE 1

FIG. 2 is a block diagram of a system 19 for simulating a system 10. The system 19 includes a user interface 20, a modeling and simulation module 22, a data storage and retrieval module 24, a libraries 26, and a user data files 28. The user interface 20 is connected to the modeling and simulation module 22. The modeling and simulation module 22 is connected to the data storage and retrieval module 24. The data storage and retrieval module 24 is connected to the libraries 26 and the user data files 28.

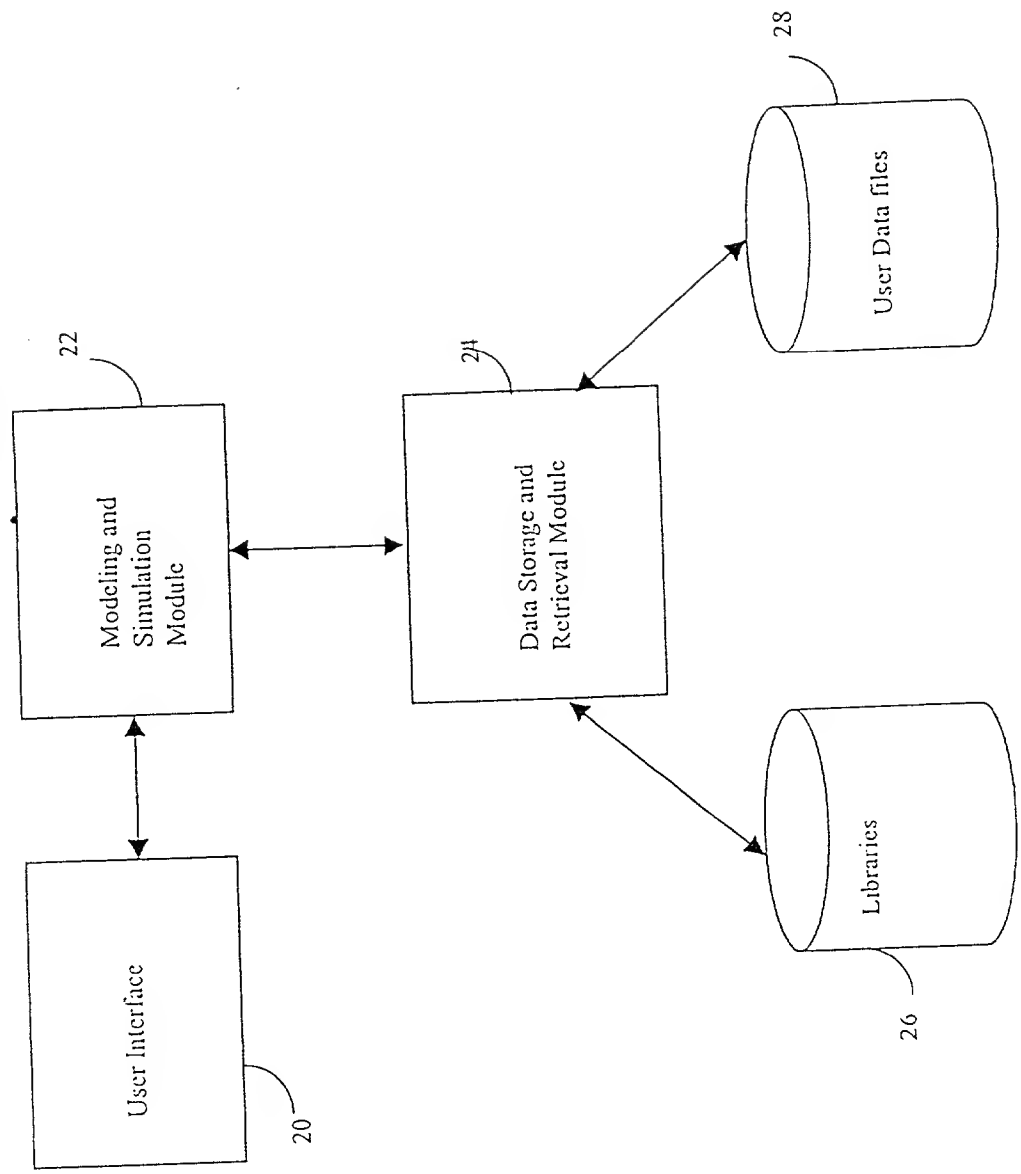


FIGURE 2

FIGURE 3, 54

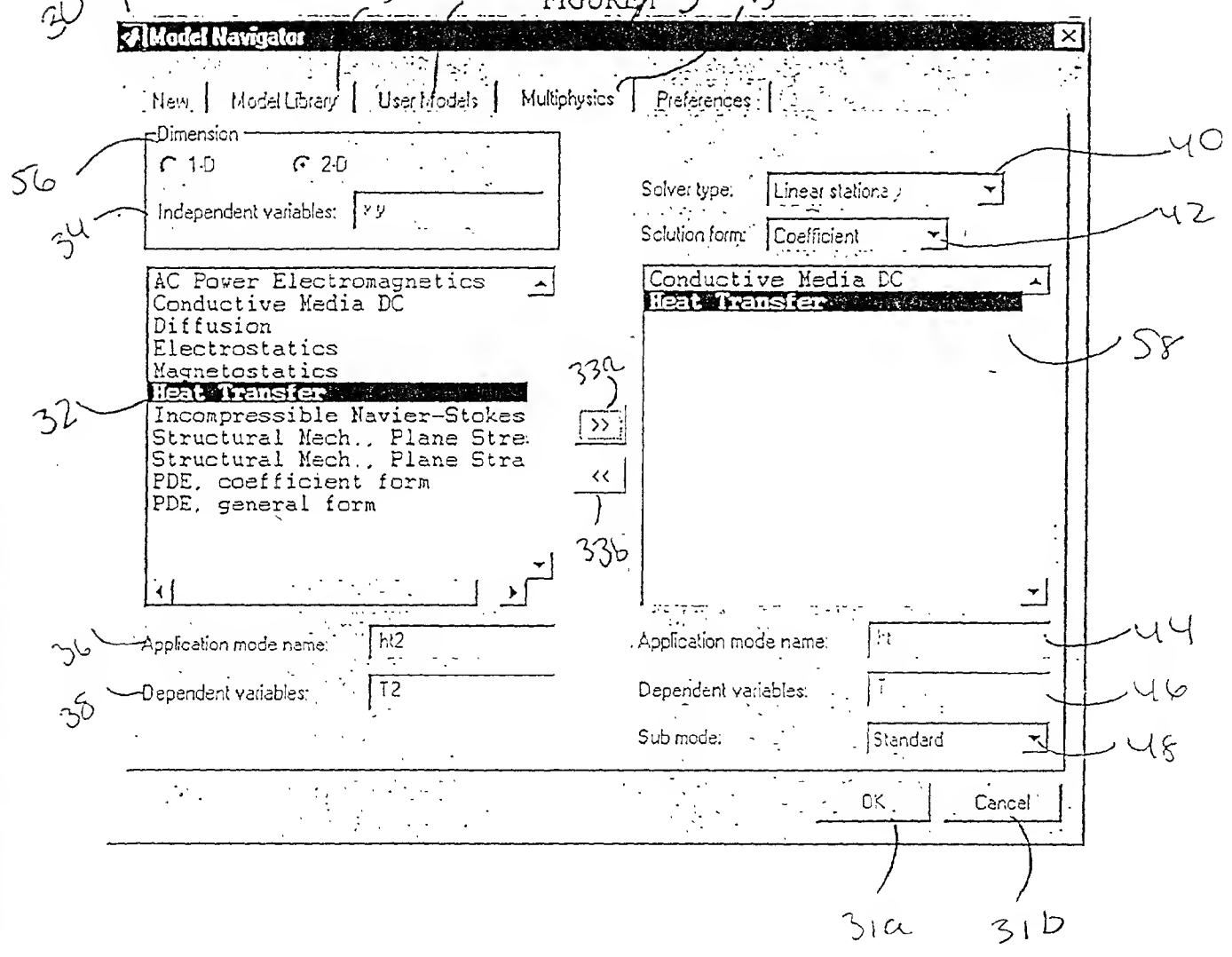


FIGURE 4

**PDE Specification/ht**

Equation:  $p \cdot C \cdot T' \cdot \nabla \cdot (k \nabla T) = Q + h(T_{\text{ext}} - T) + C_{\text{trans}}(T_{\text{ambtrans}} - T)$ .  $T$  = temperature

Subdomain selection

1

Name: 1

☒ Active in this subdomain

PDE coefficients ☒ Unlock

Coefficient	Value	Description
$p$	8930	Density
$C$	340	Heat capacity
$k$	384	Coeff. of heat conduction
$Q$	$1./((10*(1+\alpha*(T-T0))))$	Heat source
$h_{\text{trans}}$	0	Convect. heat transf. coeff.
$T_{\text{ext}}$	0	External temperature
$C_{\text{trans}}$	0	User-defined constant
$T_{\text{ambtrans}}$	0	Ambient temperature

☒ On top

OK Cancel Apply

Figure 4: PDE Specification/ht dialog box. The dialog box is titled "PDE Specification/ht". It contains a text area for the equation, a subdomain selection list, a name field, an "Active in this subdomain" checkbox, a table of PDE coefficients, and buttons for "On top", "OK", "Cancel", and "Apply".

70

FIGURE 7.5

**Boundary Conditions**

Equation:  $T = T_0$

Boundary selection

1

2

3

4

5

6

7

Name: 1

☐ Enable borders

Boundary coefficients ☒ Unlock

Quantity	Value	Description
<input type="radio"/> q	0	Heat flux
<input type="radio"/> h	0	Heat transfer coefficient
<input type="radio"/> T <sub>inf</sub>	0	External temperature
<input type="radio"/> C	0	Problem-dependent constant
<input type="radio"/> T <sub>amb</sub>	0	Ambient temperature
<input type="radio"/> n · (k · grad T) = 0		Insulation/symmetry
<input checked="" type="radio"/> T	300	Temperature
<input type="radio"/> T = 0		Zero temperature

☒ On top

OK

Cancel

Apply

72

72b

72a

74a

74

74b

— continued —

92c

☒ On top

FIG. 6A is a block diagram of a system architecture for a femtosecond laser system. The system includes a femtosecond laser 250, a control unit 252, a data storage unit 254, a data processing unit 256, a data output unit 258, a data input unit 260, a data processing unit 262, a data output unit 264, a data input unit 266, a data processing unit 268, and a data output unit 270.

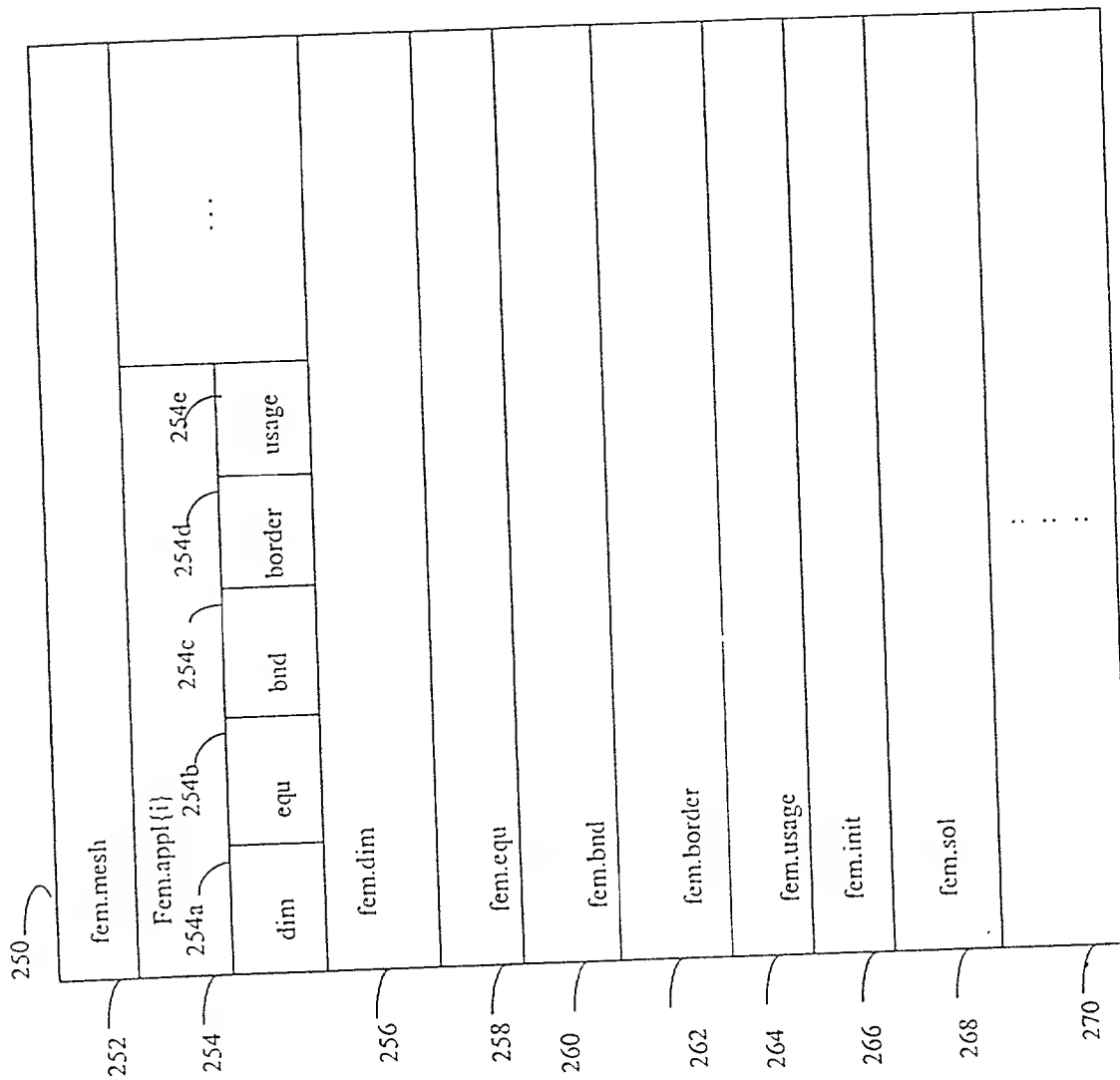


Figure 6A

FIGURE 5/7

**Solver Parameters**

General | Adaption | Nonlinear | Timestepping | Eigenvalue | Multigrid | Multiphysics

Solve for variables

☒ Show variables

**Structural Mechanics, Plane Stress (ps)**

**Heat Transfer (hl)**

Update mechanism for initial value u

Update u

☒ Update u automatically

☒ Use interpolation

Use solution number 1

Solve OK Cancel Apply

114a

124

112

116

116d

118a

118b

118c

118d



FIGURE 8

$$\left. \begin{aligned}
 & d_{a\ l k} \frac{\partial u_k}{\partial t} - \frac{\partial}{\partial x_j} \left( c_{l k j i} \frac{\partial u_k}{\partial x_i} + \alpha_{l k j} u_k - \gamma_{l j} \right) + \beta_{l k i} \frac{\partial u_k}{\partial x_i} + a_{l k} u_k = f_l \quad \Omega \quad 142 \\
 & n_j \left( c_{l k j i} \frac{\partial u_k}{\partial x_i} + \alpha_{l k j} u_k - \gamma_{l j} \right) + q_{l k} u_k = g_l - h_{m l} \lambda_m \quad \left. \begin{aligned} & 146a \\ & \partial \Omega \\ & 146b \\ & \partial \Omega \end{aligned} \right\} 146 \\
 & h_{m l} u_l = r_m
 \end{aligned} \right\} 140$$

FIGURE 9

$$\left. \begin{aligned}
 & d_{a\ l k} \frac{\partial u_k}{\partial t} + \frac{\partial \Gamma_{l j}}{\partial x_j} = F_l \quad \Omega \quad 152 \\
 & -n_j \Gamma_{l j} = G_l + \frac{\partial R_m}{\partial u_l} \lambda_m \quad \left. \begin{aligned} & \partial \Omega \quad 154a \\ & \partial \Omega \quad 154b \end{aligned} \right\} 154 \\
 & 0 = R_m
 \end{aligned} \right\} 150$$

$$\begin{array}{l}
 \gamma_{ij} = \Gamma_{ij} \\
 c_{ijkj} = - \frac{\partial \Gamma_{ij}}{\partial \left( \frac{\partial u_k}{\partial x_i} \right)} \\
 \beta_{lki} = - \frac{\partial F_l}{\partial \left( \frac{\partial u_k}{\partial x_i} \right)} \\
 g_l = G_l \\
 q_{lk} = - \frac{\partial G_l}{\partial u_k}
 \end{array}
 \quad
 \begin{array}{l}
 f_l = F_l \\
 \alpha_{lkj} = - \frac{\partial \Gamma_{lj}}{\partial u_k} \\
 a_{lk} = - \frac{\partial F_l}{\partial u_k} \\
 r_l = R_l \\
 h_{lk} = - \frac{\partial R_l}{\partial u_k}
 \end{array}$$

Figure 10

FIGURE 11

$$240 \left\{ \begin{array}{l} \Gamma_{lj} = -c_{lkji} \frac{\partial u_k}{\partial x_i} - \alpha_{lkj} u_k + \gamma_{lj} \\ F_l = f_l - \beta_{lki} \frac{\partial u_k}{\partial x_i} - a_{lk} u_k \\ G_l = g_l - q_{lk} u_k \\ R_m = r_m - h_{ml} u_l \end{array} \right.$$

FIG 12

$$\begin{aligned}
 & \int_{\Omega} \left( \left( c_{lkji} \frac{\partial u_k}{\partial x_i} + \alpha_{lkj} u_k \right) \frac{\partial v}{\partial x_j} + \left( d_{alk} \frac{\partial u_k}{\partial t} + \beta_{lki} \frac{\partial u_k}{\partial x_i} + a_{lk} u_k \right) v \right) dx + \\
 & \int_{\partial\Omega} q_{lk} u_k v ds = \int_{\Omega} \left( \gamma_{lj} \frac{\partial v}{\partial x_j} + f_l v \right) dx + \int_{\partial\Omega} (g_l - h_{ml} \lambda_m) v ds \\
 & \int_{\partial\Omega} \mu h_{mk} u_k ds = \int_{\partial\Omega} \mu r_m ds
 \end{aligned}$$

FIG 13

$$302 \left\{ \begin{array}{l} \int_{\Omega} \left( \Gamma_{lj} \frac{\partial v}{\partial x_j} + F_l v - d_{alk} \frac{\partial u_k}{\partial t} v \right) dx + \int_{\partial\Omega} \left( G_l + \frac{\partial R}{\partial u_l} \lambda_m \right) v ds = 0 \\ \int_{\partial\Omega} R_m \mu ds = 0 \end{array} \right.$$

FIG 14

$$364 \left\{ U_k(x) = \sum_{I=1}^{N_p} U_{I,k} \phi_I(x), \right.$$

$$\Lambda_m(x) = \sum_{K=1}^{N_s} \sum_{L=1}^n \Lambda_{K,L,m} \psi_{K,L}(x)$$

FIG 15

$$2U_6 \left\{ \begin{aligned} & \int_{\tau} \left( c_{lkji} U_{I,k} \frac{\partial \phi_I}{\partial x_i} + \alpha_{lkj} U_{I,k} \phi_I \right) \frac{\partial \phi_J}{\partial x_j} dx + \\ & \int_{\tau} \left( d_{alk} \frac{\partial U_{I,k}}{\partial t} \phi_I + \beta_{lki} U_{I,k} \frac{\partial \phi_I}{\partial x_i} + a_{lk} U_{I,k} \phi_I \right) \phi_J dx + \\ & \int_{\partial \tau} q_{lk} U_{I,k} \phi_I \phi_J ds = \int_{\tau} \left( \gamma_{lj} \frac{\partial \phi_J}{\partial x_j} + f_l \phi_J \right) dx + \\ & \int_{\partial \tau} (g_l - h_{ml} \Lambda_{K,L,m} \psi_{K,L}) \phi_J ds \end{aligned} \right.$$

$$\gamma_0 \int_{\partial \Sigma} h_{mk} U_{l,k} \phi_l \Psi_{K,L} ds = \int r_m \Psi_{K,L} ds$$

FIG 16



FIG 17

$$3^{12} \left\{ \int_{\tau} \left( \Gamma_{lj} \frac{\partial \phi_j}{\partial x_j} + F_l \phi_j - d_{alk} \frac{\partial u_k}{\partial t} \phi_j \right) dx + \int_{\partial \tau} \left( G_l + \frac{\partial R_m}{\partial u_l} \Lambda_{K,L,m} \Psi_{K,L} \right) \phi_j ds = 0 \right. \\ \left. \int_{\partial \tau} R_m \Psi_{K,L} ds = 0 \right.$$

FIG 18

$$\begin{aligned}
310 \quad DA_{(J,l),(I,k)} &= \int_{\tau} d a_{lk} \phi_I \phi_J dx \\
C_{(J,l),(I,k)} &= \int_{\tau} c_{lkji} \frac{\partial \phi_I}{\partial x_i} \frac{\partial \phi_J}{\partial x_j} dx \\
AL_{(J,l),(I,k)} &= \int_{\tau} \alpha_{lkj} \phi_I \frac{\partial \phi_J}{\partial x_j} dx \\
BE_{(J,l),(I,k)} &= \int_{\tau} \beta_{lki} \frac{\partial \phi_I}{\partial x_i} \phi_J dx \\
A_{(J,l),(I,k)} &= \int_{\tau} a_{lk} \phi_I \phi_J dx \\
Q_{(J,l),(I,k)} &= \int_{\partial \tau} q_{lk} \phi_I \phi_J ds \\
GA_{(J,l)} &= \int_{\tau} \gamma_{lj} \frac{\partial \phi_J}{\partial x_j} dx \\
F_{(J,l)} &= \int_{\tau} f_l \phi_J dx \\
G_{(J,l)} &= \int_{\partial \tau} g_l \phi_J ds \\
H_{(K,L,m),(I,k)} &= \int_{\partial \tau} h_{mk} \phi_I \Psi_{K,L} ds \\
R_{(K,L,m)} &= \int_{\partial \tau} r_m \Psi_{K,L} ds
\end{aligned}$$

FIG 19

$$\left\{ \begin{array}{l} DA \frac{\partial U}{\partial t} + (C + AL + BE + A + Q)U + H^T \Lambda = GA + F + G \\ HU = R \end{array} \right.$$

FIG 20

$$\left\{ \begin{array}{l} DA \frac{\partial U}{\partial t} + H^T \Lambda = GA + F + G \\ R = 0 \end{array} \right.$$

FIG 21

$$326 \quad \begin{cases} J(U^{(k)}) \Delta U^{(k)} = -\rho(U^{(k)}) \\ U^{(k+1)} = U^{(k)} + \lambda_k \Delta U^{(k)} \end{cases}$$

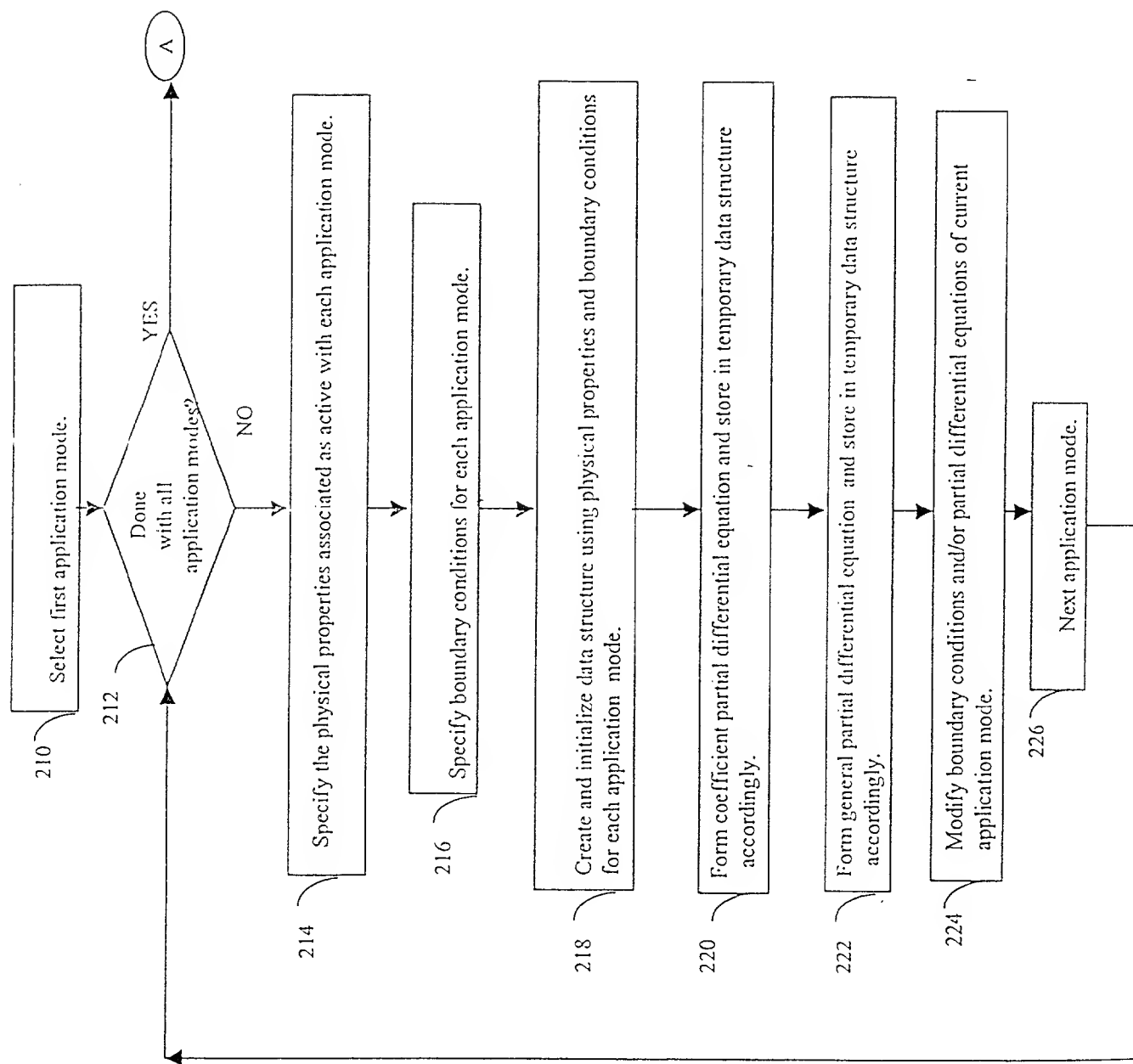


Figure 22

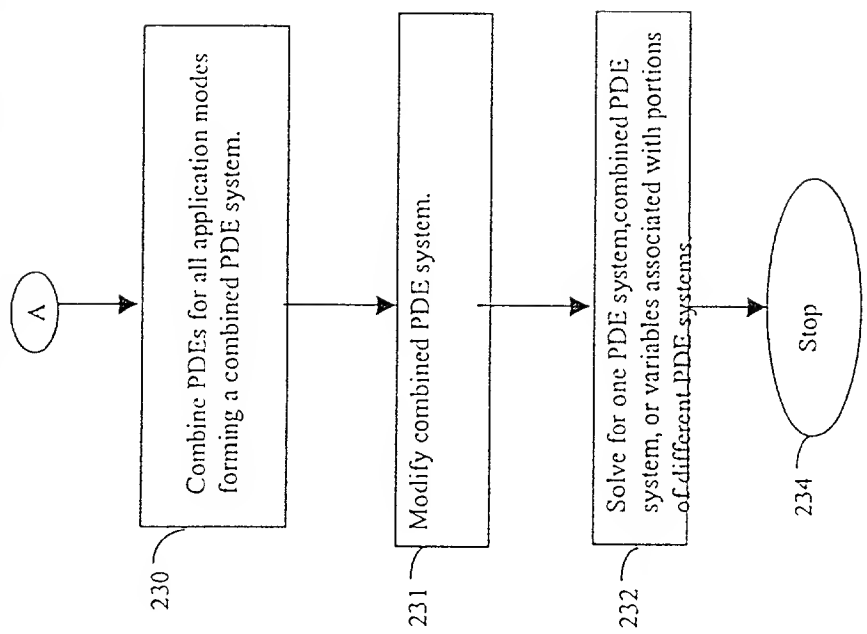
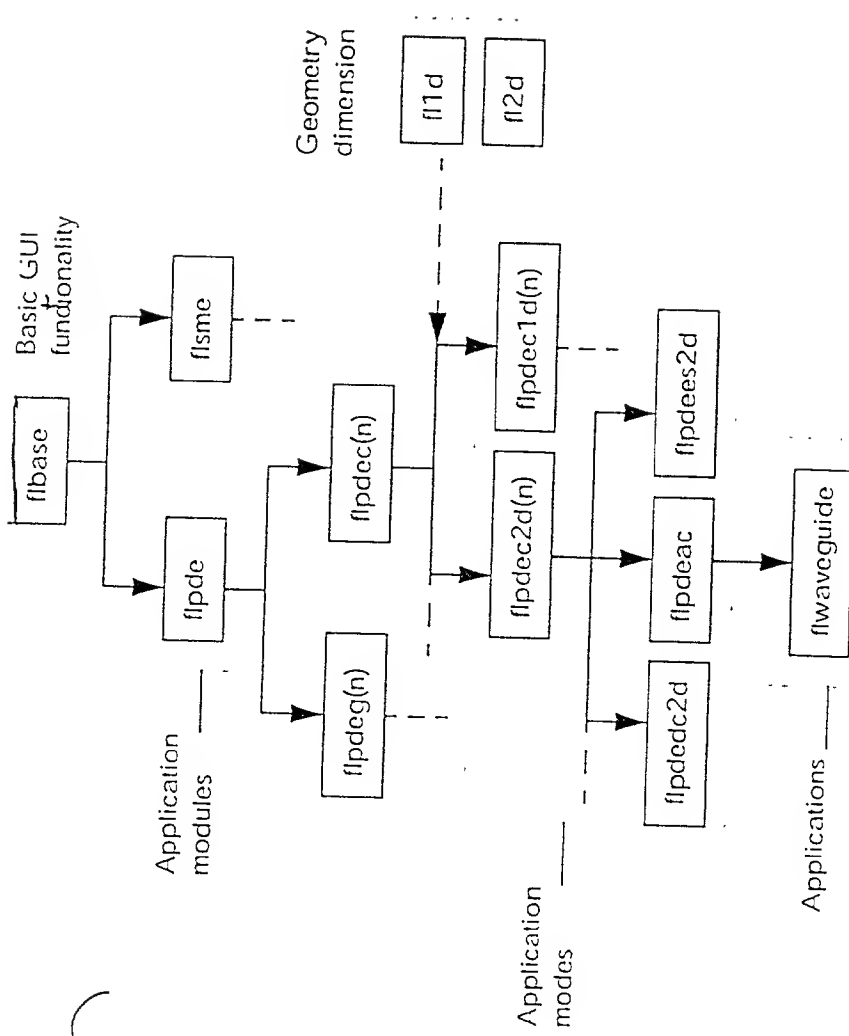


FIGURE 23

The class hierarchy of FEMLAB  
 is shown in Figure 24.



The class hierarchy of FEMLAB

Figure 24



### 1-D Physics Application Modes

Application mode	Class name	Parent class
Diffusion	flpdedf1d	flpdedf
Heat Transfer	flpdeht1d	flpdeht

S02

### : 1-D PDE Application Modes

Application mode	Class name	Parent class
Coefficient PDE model, n variables	flpdec1d(n)	flpdec(n)
General PDE model, n variables	flpdeg1d(n)	flpdeg(n)

S04

FIGURE 25

Figure 26 shows the hierarchy of the 2-D Physics Application Modes. The modes are organized into two main categories: Sub and Sol.

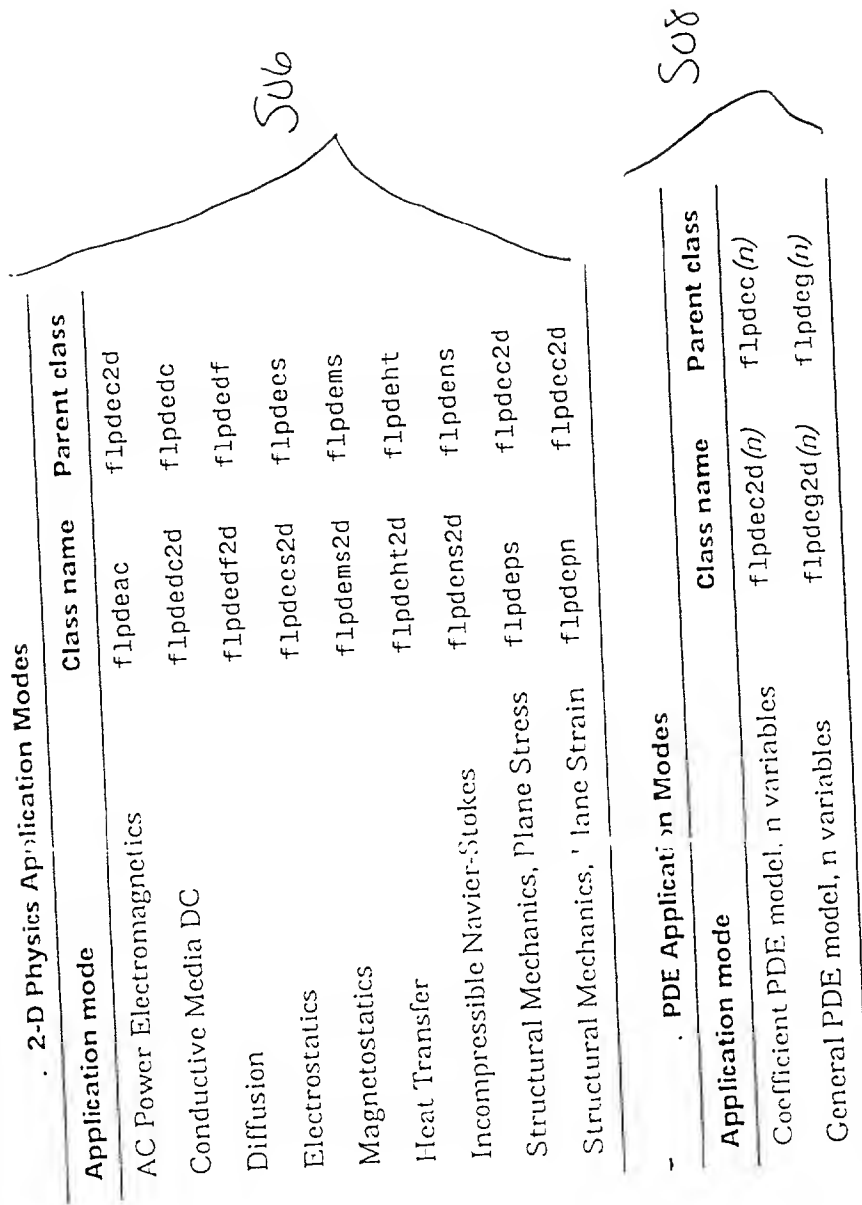


FIGURE 26

Application Object Properties

Property name	Description	Data type
dim	Names of the dependent variables	Cell array of strings
form	PDE form	String (coefficient/general)
name	Application name	String
parent	Parent class names	String, cell array of strings, or the empty matrix
sdim	Names of the independent variables (space dimensions)	Cell array of strings
submode	Name of current submode	String (std/wave)
tdiff	Time differentiation flag	String (on/off)

FIGURE 27

510

```
function obj = myapp()
%MYAPP Constructor for a FEMLAB application object.
obj.name = 'My first FEMLAB application';
obj.parent = 'flpdeht2d';

% MYAPP is a subclass of FLPDEHT2D:
p1 = flpdeht2d;
obj = class(obj,'myapp',p1);
set(obj,'dim',default_dim(obj));
```

FIGURE 28

512

### Physics Modeling Methods

Function	Purpose
appspect	Return application specifications.
bnd_compute	Convert application-dependent boundary conditions to generic boundary coefficients.
default_bnd	Default boundary conditions.
default_dim	Default names of dependent variables.
default_equ	Default PDE coefficients/Material parameters.
default_init	Default initial conditions.
default_sdim	Default space dimension variables.
default_var	Default application scalar variables.
dim_compute	Return dependent variables for an application.
equ_compute	Convert application-dependent material parameters to generic PDE coefficients.
form_compute	Return PDE form.
init_compute	Convert application-dependent initial conditions to generic initial conditions.
posttable	Define assigned variable names and post-processing information.

FIGURE 29

When you click on the "Model Navigator" button, the "Model Navigator" dialog box appears. The "Model Navigator" dialog box contains the following information:

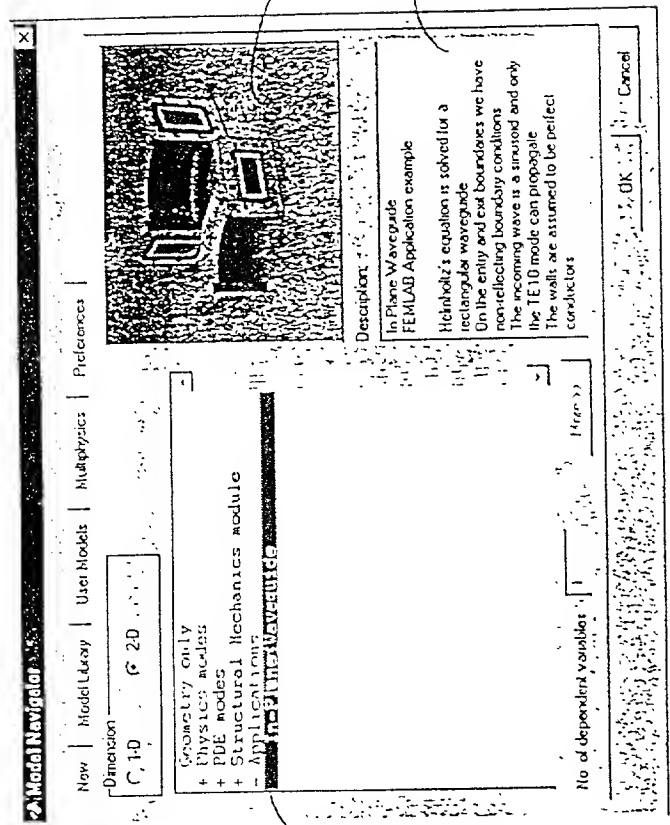


FIGURE 30

$$S32 \left[ \Delta E_z + (2\pi i k)^2 E_z = 0 \right.$$

$$S32 \left[ k = \frac{1}{\lambda} = \frac{f}{c} \right.$$

$$S34 \left[ \vec{n} \cdot (\nabla E_z) + 2\pi i k_x E_z = 4\pi i k_x \sin\left(\frac{\pi}{d}(y - y_0)\right) \right.$$

$$S36 \left[ k^2 = k_x^2 + k_y^2 \right.$$

$$S38 \left[ k_x = \sqrt{\frac{1}{\lambda^2} - \frac{1}{(2d)^2}} \right.$$

$$S40 \left[ \vec{n} \cdot (\nabla E_z) + 2\pi i k_x E_z = 0 \right.$$

$$S42 \left[ E_z = 0 \right.$$

$$S44 \left[ f_c = \frac{c}{2d} \right.$$

FIGURE 31

550

```

function obj = flwaveguide(varargin)
%FLWAVEGUIDE Constructor for a Waveguide application object.

obj.name = 'In-Plane Waveguide';
obj.parent = 'flpdeac';

% FLWAVEGUIDE is a subclass of FLPDEAC:
p1 = flpdeac;
obj = class(obj,'flwaveguide',p1);
set(obj,'dim',default_dim(obj));

```

FIGURE 32

552

fem.user fields	
Field	Description
geomparam	1-by-2 structure of geometry parameters.
entrybnd	Index to the entry boundary.
exitbnd	Index to the exit boundary.
freqs	Frequency vector

FIGURE 33

554

fem.user fields	
Field	Description
startpt	Index of the lower left corner point of the waveguide.
type	Type of waveguide. ('straight' or 'elbow')

FIGURE 34

556

geomparam fields			
Field	Description	Defaults for elbow	Defaults for straight
entrylength	Length of the entrance part of the waveguide.	0.1	0.1
exitlength	Length of the exit part of the waveguide.	0.1	Not used
radius	Outer radius of the waveguide bend.	0.05	Not used
width	Width of the waveguide.	0.025	0.025
cavityflag	Turn resonance cavity on or off.	0	0
cavitywidth	Width of the resonance cavity.	0.025	0.025
postwidth	Width of the protruding posts.	0.005	0.005
postdepth	Depth of the protruding posts.	0.005	0.005

FIGURE 35



614 —————

604

606

608

610

600

612/612a

620

622

616

618

624

626

Figure 36

Model Navigator

New | Model Library | User Module | Multiphysics | Preferences

Geometry name: Geom1 Add 612/612a 620

Dimension: 2D 3D 602

Independent variables: XYZ

Solver type: Time dependent

Solution form: General 622

Geom1: Conductive media DC

Geom1: Heat transfer

Conductive media DC

Diffusion

Electrostatics

Magnetostatics

Heat transfer

Incompressible Navier-Stokes

Structural mechanics

PDE, coefficient form

PDE, general form

Weak, subdomain

Weak, boundary

Weak, edge

Weak, point

Weak, boundary constraint

Application mode name: h12

Dependent variables: T2 616

Element: Lagrange - Quadratic

Application mode name: h1

Dependent variables: T 624

Submode: Standard

OK Cancel

**Boundary Settings (ci)**

Equation:  $n \cdot (c \nabla u + u \gamma) + q u = g \cdot h^T \mu h u = f$

**Coefficients** | **Weak**

Domain selection: ☐ 1 ☐ 2 ☐ 3 ☐ 4

**Weak complement** ☒ **Unlock**

Term	Value	Description
weak	0	Weak term
dweak	0	Time-dep. weak term
constr	0	Constraint

Name: 1

☐ Select by group

☐ Enable borders

☒ On top

OK Cancel Apply

Figure 37

Subdomain Settings/as

Equation:  $\nabla \cdot (\epsilon \nabla V/P) = \rho$ ,  $E = -\nabla V$ ,  $V = \text{electric potential}$

Coefficients

Init

Element

802

Domain selection

2

Name: 1

☐ Select by group

☒ Active in this domain

Element settings

☒ Use default element

Lagrange - Quadratic

Coefficient	Value	Description
shapeo	shlag(2,V)	Shape function
gporder	4	Integration order
cporder	2	Constraints order

☒ On top

OK

Cancel

Apply

800

Figure 38

**Subdomain Settings/CI**

Equation:  $\nabla \cdot (c \nabla u - \alpha \nabla u) + \alpha u + \beta \nabla u = f$

Coefficients | Init | Element | Weak |

Domain selection: 1 2

Weak complement ☒ Unlink

Term	Value	Description
weak	0	Weak term
dweak	0	Time-dep. weak term
constr	0	Constraint

Name: 1

☐ Select by group

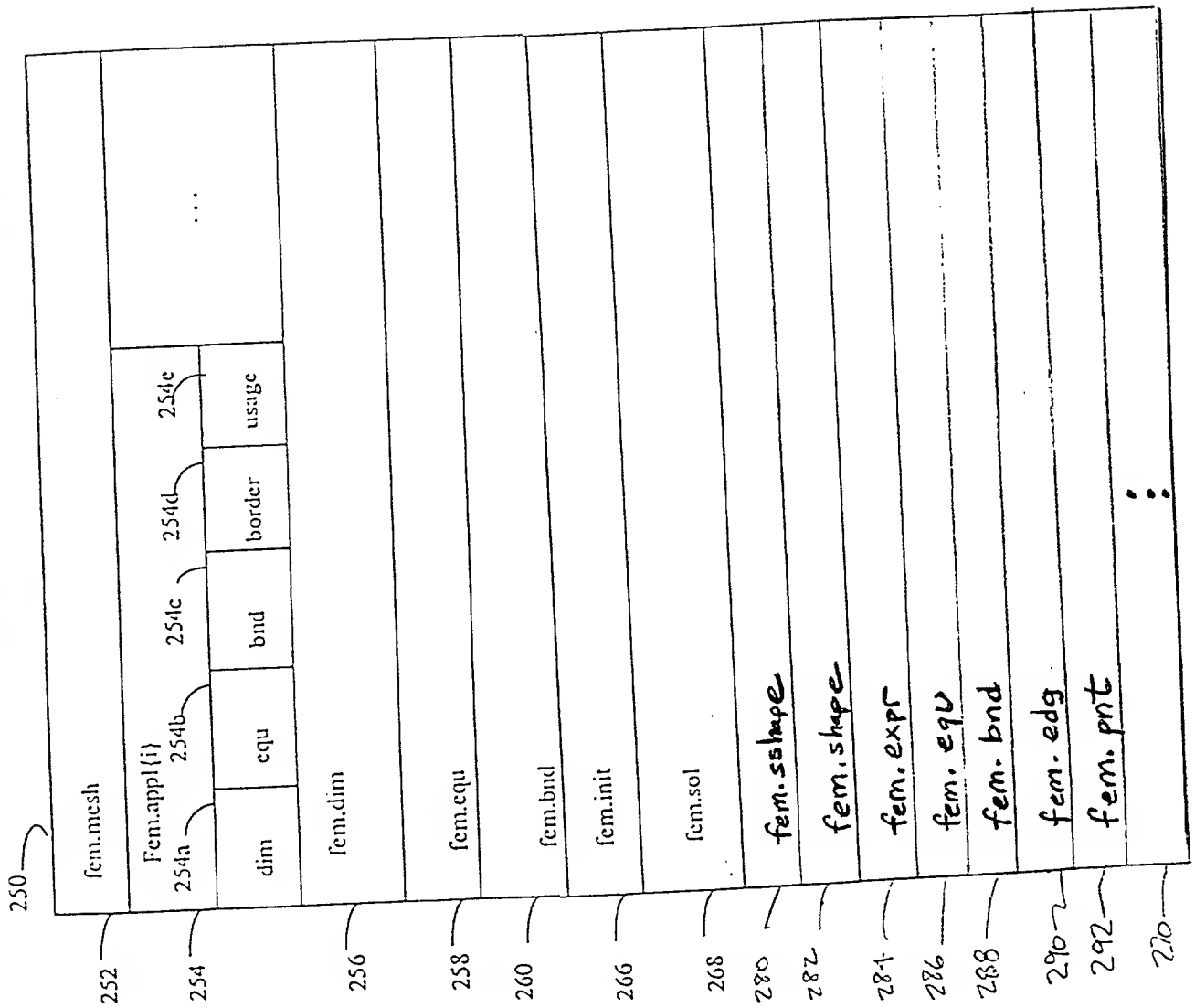
☒ Active in this domain

☒ On top

OK Cancel Apply

Figure 39

↑ 900



1000

Figure 40

$$\left\{ \begin{aligned}
 0 &= \int_{\Omega} W^{(2)} dA + \int_B W^{(1)} ds + \sum_P W^{(0)} + \\
 &+ \int_{\Omega} \frac{\partial R_m^{(2)}}{\partial u_l} \mu_m^{(2)} dA + \int_B \frac{\partial R_m^{(1)}}{\partial u_l} \mu_m^{(1)} ds + \sum_P \frac{\partial R_m^{(0)}}{\partial u_l} \mu_m^{(0)}
 \end{aligned} \right.$$

1104

$0 = R^{(2)}$  on  $\Omega$   
 $0 = R^{(1)}$  on B  
 $0 = R^{(0)}$  on P

1100  
 Figure 41

$$W_l^{(n)} = W_l^{(n)} + \Gamma_{lj} \frac{\partial v_l}{\partial x_j} + F_l v_l$$

$$W_l^{(n)} = W_l^{(n)} + d_{alk} \frac{\partial u_k}{\partial t} v_l$$

$$W_l^{(n-1)} = W_l^{(n-1)} + G_l v_l$$

$$R_m^{(n)} = R_m$$

1200

Figure 42

**Point Settings/CI**

Domain selection

1 2 3 4 5 6 7 8

Name: 1

☐ Select by group

Weak complement ☒ Weak

Term	Value	Description
weak	0	Weak term
dweak	0	Time-dep. weak term
constr	0	Constraint

☒ On top

OK

Cancel

Apply

Figure 43



Edge settings/c1

Domain selection: ☐ 1 ☐ 2 ☐ 3 ☐ 4 ☐ 5 ☐ 6 ☐ 7 ☐ 8

Name:  ☐ Select by group

Weak complement ☒ (default)

Term	Value	Description
weak	0	Weak term
dweak	0	Time-dep. weak term
constr	0	Constraint

1408

☒ On top ☐ OK

Figure 4

1500A →

**Coupling Variable Settings**

Variables | Source | Destination

Name: Type: Defined from → Available in:

Name	Type	Defined from	Available in
c1	scalar	Geom1:sub	→ Geom2: bnd
c2	extr	Geom1: bnd	→ Geom1: pnt

1502 Variable name: c2

1504 Variable type: extrusion

1506 Add

1508 Delete

☒ On top

OK Cancel Apply

Figure 45A

1500 →

1500B

**Coupling Variable Settings**

Variables | Source | Destination

Variable: c2

Domain selection

Geometry:

Level:

☐ Select by group

Definition ☒ Copy from 3

Expression:

Integration order:

Local mesh transformation:

	x	y	z
1510a	<input type="text"/>	<input type="text"/>	<input type="text"/>
1510b	<input type="text"/>	<input type="text"/>	<input type="text"/>
1510c	<input type="text"/>	<input type="text"/>	<input type="text"/>

☒ On top

1502

1504

1506

1508

Figure 45B

1500

TOP SECRET 1500

**Coupling Variable Settings**

Variables | Source | Destination

Variable: c2

Domain selection

Geometry:

Level:

☒ Select by group

2 3 4 5 6 7 8

Definition ☒ Copy from

☐ Select within domain

Evaluation point transformation:

x y z

1572a 1572b 1572c

☒ On top           

1500

Figure 45c

**Expression Variable Settings**

**Variables** | **Definition**

Name:	Type:	Defined in:
em_s	subdomain	Geom1:sub
we	geometry	Geom2

Variable name:

Variable type:

☒ On top

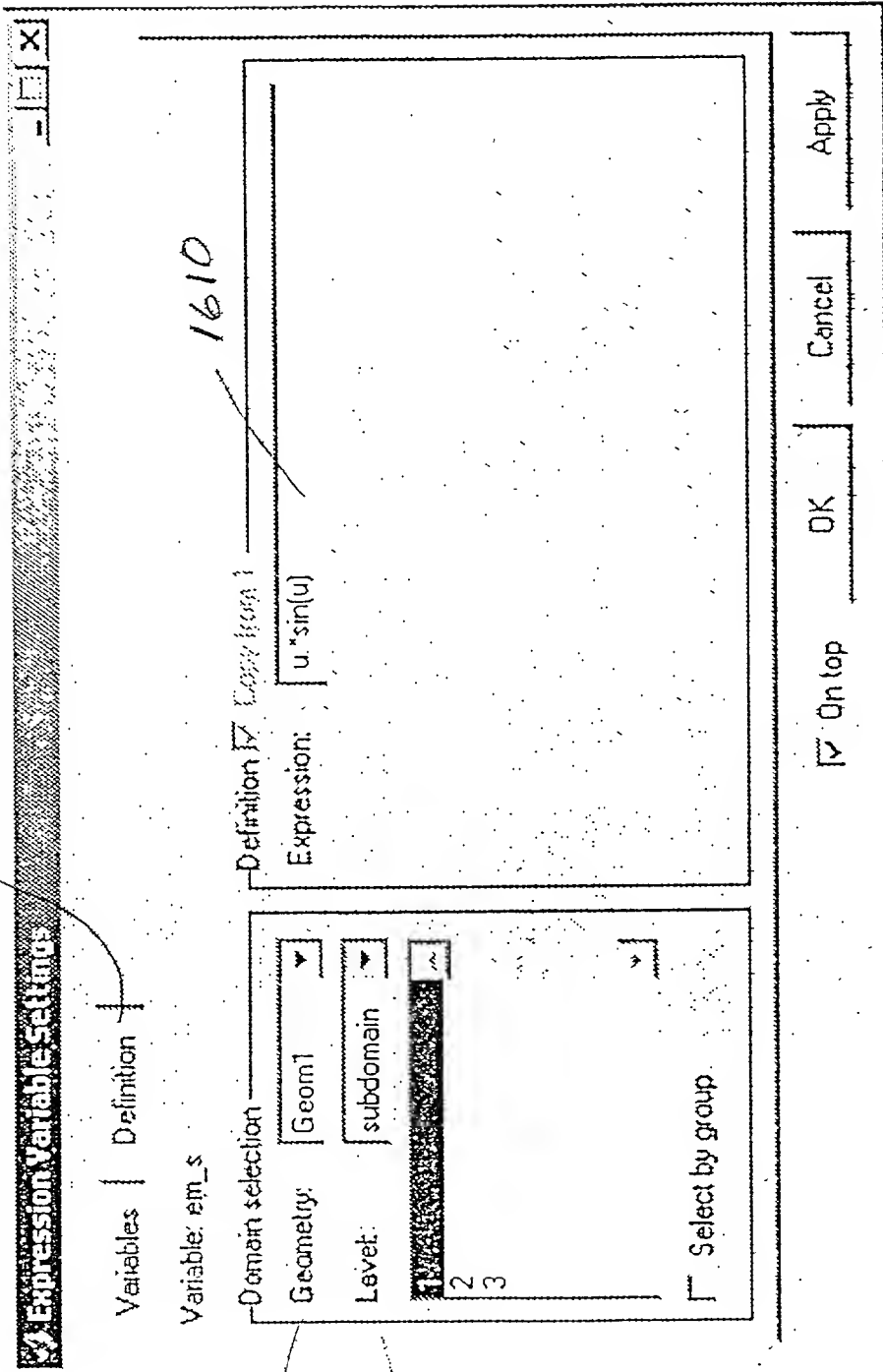
1600A

1602

1604

1600

Figure 46



1600

Figure 47

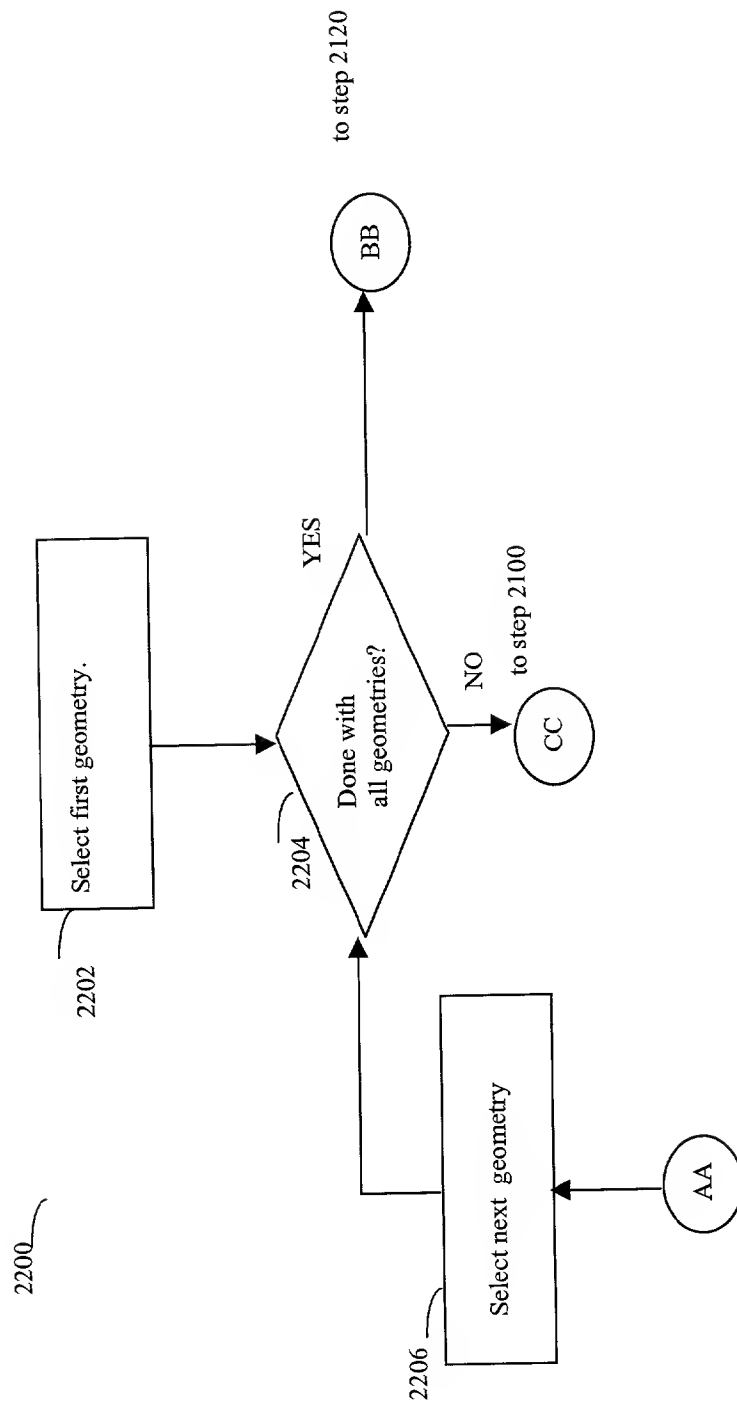


FIGURE 48

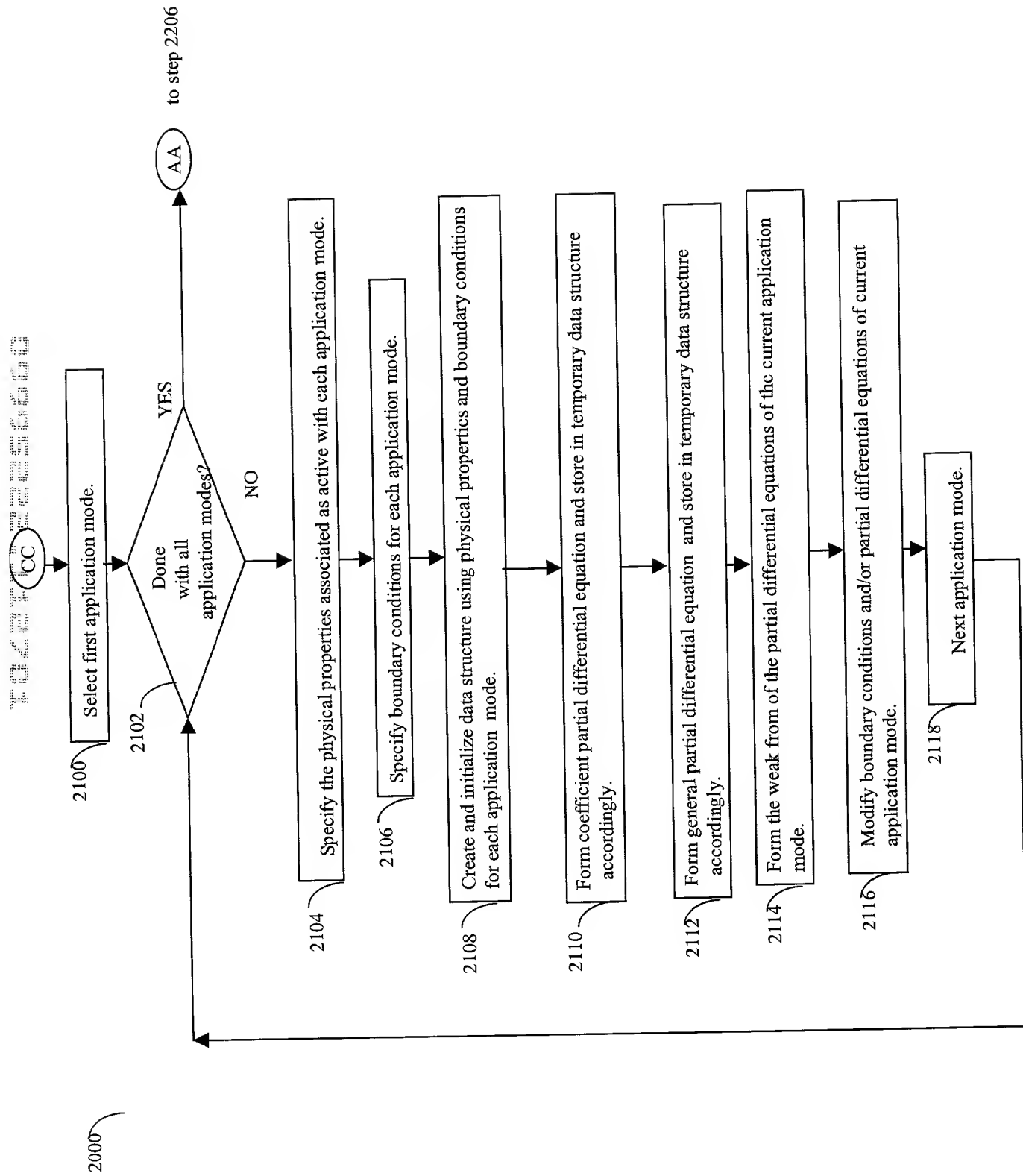


FIGURE 49



various other aspects of the present invention are apparent from the description and the drawings.

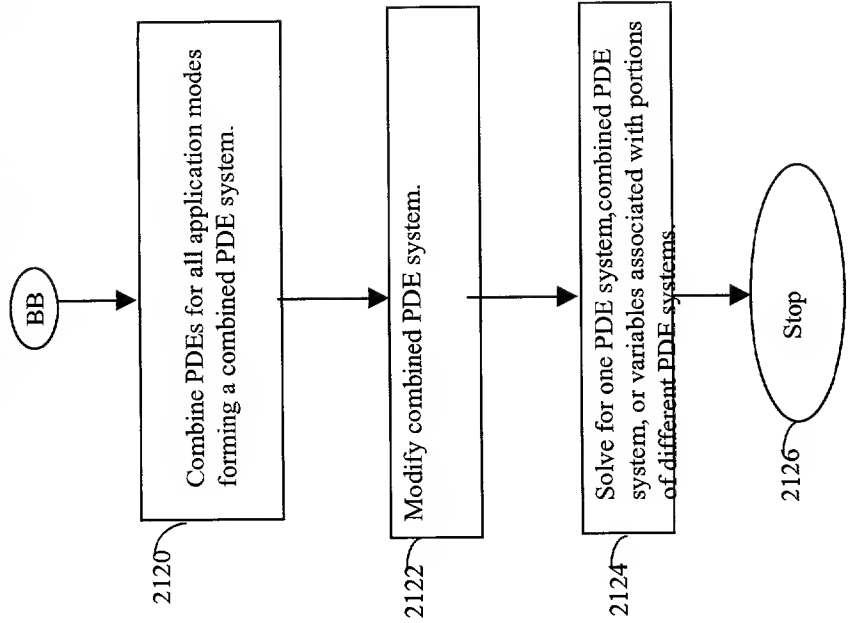


FIGURE 50